Thoughts on Teaching C++ to Students in the Applied Sciences

NWCPP Meeting, 15 April 2020
To the crew of Apollo 13, and all the members of Mission Control who worked tirelessly to get the men home safely, 50 years ago this month.

Dedication

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• Single quarter introductory/intermediate course (10 weeks) in C++ for MSc students in Computational Finance & Risk Management (CFRM) at the University of Washington

• Emphasis on applications

• ~90% of this material would be transferable to general applied sciences

• Orders of magnitude more efficient than Python

• But can be almost as rapid to develop, thanks to *modern* C++

• Currently in sixth year of teaching this course
• Companion lecture notes: *C++ for the Rest of Us!*
• Introductory:
  ➢ Fundamentals of C++
  ➢ Object-Oriented Programming
  ➢ Templates
  ➢ STL Containers and Algorithms

• Intermediate:
  ➢ Prior programming experience in other languages is assumed
    • Functions
    • Conditional branching
    • Iteration
    • We move very quickly through these topics
  ➢ Open source mathematical libraries
  ➢ By the end of the quarter, students are able to implement some fairly sophisticated mathematical routines and models
• Proficiency in implementing common mathematical models in C++
• Emphasis on modern (through C++17) language and Standard Library features for problem solving
  • “No-cost” abstractions
  • Don’t reinvent what we already have
  • Don’t discourage students with gratuitously complicated code or legacy C constructs
  • Use modern C++ for practical work!
  • Bust the myth that C++ is “too difficult”
• C language programming
  • Not a prerequisite
  • `std::string`, not `char*`
  • `std::vector<>`, not dynamic C-arrays

• Minute details about strings and output formatting
  • Computational course, so we care more about numerical results
  • In practice, results are not output to the console with `std::cout`

• The multitude of numerical types in C++; we only require the following for our work
  • `double`
  • `int`
  • `size_t` and `long` where necessary
• Memory allocation with `new` and `delete`
  • We use `std::unique_ptr<.>` instead
  • `new` and `delete` are covered during the last week

• Implementing sort/search algorithms or doubly-linked lists
  • They’re in the Standard, so use them
  • We use `std::vector<.>` anyway
• A brief history of C++
  • “The Creator” Bjarne Stroustrup
  • Turn of the century heyday (c 1998-2008)
  • Stagnation: C++98/C++03 and the emergence of Java
  • The Beast is Back (Jon Kalb): C++11 and the post-2011 world

• IDE project setup
  • Visual Studio 2019 is preferred
  • How to build a simple executable
  • Compiler warnings and errors
• Math
  • Numerical variables: \texttt{int} and \texttt{double}
  • Math operators
  • Mathematical functions in \texttt{<cmath>}

• User-defined functions
  • Declaration and implementation
  • Write own functions using \texttt{<cmath>}

Week 1 (continued)
• Classes and objects
  • Car is a class, a Dino Ferrari 308 GT4 and a Honda Accord are objects

• Member variables and member functions
• UML class diagrams

<table>
<thead>
<tr>
<th>Car</th>
<th>What it is</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wheels</td>
<td>(name of class)</td>
</tr>
<tr>
<td>Engine</td>
<td></td>
</tr>
<tr>
<td>Body</td>
<td></td>
</tr>
<tr>
<td>Brakes</td>
<td></td>
</tr>
<tr>
<td>Accelerator</td>
<td></td>
</tr>
<tr>
<td>Move forward</td>
<td>What it has</td>
</tr>
<tr>
<td>Stop</td>
<td>(attributes, aka member variables)</td>
</tr>
<tr>
<td>Turn</td>
<td></td>
</tr>
</tbody>
</table>

| What it does (methods, aka member functions) |             |
|                                             |             |
• Classes and objects (continued)
  • `std::string` as an example
    ➢ What it means to create an instance
    ➢ Call and use the member functions
      • `at(.)`
      • `size(.)`
      • `push_back(.)`
    • These also then become more familiar for when we cover STL containers

• Conditional and iterative statements
  • `if/else if/else`
  • `switch` statements
  • `for/while` loops
• Arrays
  • `std::array` and `std::vector`
  • We don’t care about dynamic C-style arrays

• Function overloading

• Aliases
  • `using`
  • prefer `using` over `typedef`
  • `(lvalue)` references

• Pointers
  • To variables on the stack
  • Only introduced here because we will soon discuss
    ➢ The `this` pointer
    ➢ STL iterators
    ➢ “Just-in-Time” approach to introducing new concepts
Modified version of the Fraction example in Josuttis – *Object Oriented Programming in C++*: Incrementally build up a class with

- Private numerator and denominator members, and public accessors and mutators for each
- Overloaded constructors
- Meaning of the `this` pointer
- Refactor error checking for zero in the denominator
  - Constructor
  - Mutator for denominator
• Fraction example (continued): Incrementally build up a class with
  • Operators
    ➢ Multiplication * and *\=, plus a common private simplifying function (uses \texttt{std::gcd(\_)} in C++17)
    ➢ Inequality <
    ➢ Equality and non-equality == and !=
    ➢ Prefix and postfix increment operators ++
    ➢ Using and returning \texttt{*this}
  • Functors
Week 3: Object-Based Programming and user-defined classes

- Fraction example – declaration file

```cpp
class FractionFour {  // Not to be confused with the Jackson 5
public:
    FractionFour();
    FractionFour(int n);
    FractionFour(int n, int d);
    void print();

    FractionFour operator * (const FractionFour& rhs) const;
    void operator *= (const FractionFour& rhs);
    bool operator < (const FractionFour& rhs) const;

    // New: increment operators:
    FractionFour operator ++ ();
    FractionFour operator ++ (int notused);

    // New: equality and non-equality operators:
    bool operator == (const FractionFour& rhs) const;
    bool operator != (const FractionFour& rhs) const;

    int numer() const;
    int denom() const;
    void setNumber(int n);
    void setDenom(int d);

    // friend operator so that we can output a fraction with cout
    // Take this as given and use it; the mechanics are beyond
    // the scope of the current topic.
    friend std::ostream& operator << (std::ostream& os, const FractionFour& rhs);
private:
    void simplify();
    int gcd() const;

    // new: private member function to check for a zero in the denominator
    void checkForZero_(int d) const;

    // new: private member to move negative sign from denominator to numerator
    void checkNegativeDenominator();

    int numer_;
    int denom_;  
};
```
• Implement a more complete set of operators on the Fraction class
  • $+$ $+=\ -\ -=\ $ (and use \texttt{std::lcm}(.)) from C++17)
  • $/$ $/=$
  • $\leq\ >\ \geq$
  • Prefix and postfix decrement
  • Other member functions
• **Inheritance**
  
  • Virtual functions
  • Virtual default destructor on base class
  • `virtual` and `override` keywords
  • Order of instantiation and destruction
  • Emphasis on abstract base interface classes
    - Pure virtual functions only
    - Restrict to one level of derivation
    - Pitfalls of extended inheritance chains
  • Polymorphism
• Assignment: inheritance and polymorphism for root-finding
  • Implement a pure abstract base class representing a function $f(x)$
    ➢ `virtual double operator()(double x) = 0 const;`
  • Implement several derived concrete classes; eg
    ➢ $ax^3 + bx^2 + cx + d$
    ➢ $a \log(x - b)$
      • Introduce and use
        `std::numeric_limits<double>::epsilon()`, `infinity()`,
        and `quiet_NaN()`
    ➢ $\gamma \sin(ax) - \eta \cos(bx)$
  • Write a function implementing a root-finding method (eg Secant) that
takes an abstract base object const reference as its argument and
computes the roots for any derived class object
Assignment: inheritance and polymorphism for root-finding (continued)

double secant(const RealFunction& rf, double x0, double x1, double tol, int maxIter) {
  double NaN = std::numeric_limits<double>::quiet_NaN();
  double root = NaN;
  double y0 = rf(x0);
  double y1 = rf(x1);
  int countIter = 0;
  for (countIter = 0; countIter <= maxIter; ++countIter) {
    if (std::abs(x1 - x0) > tol) {
      root = x1 - (x1 - x0)*y1 / (y1 - y0); // Update x1 & x0:
      x0 = x1;
      x1 = root;
      y0 = rf(x0);
      y1 = rf(x1);
    } else {
      break;
    }
  }
  if (countIter < maxIter) {
    return root;
  } else {
    return NaN;
  }
}
• **Composition** with a member object, and avoid object copy
  • Pass by and store as const *lvalue* reference
    ➢ Avoid object copy
    ➢ But not flexible
      • Lack control over lifetime of the member variable
      • Can’t modify member object after containing object initialized
      • Or copy the containing object
  • Pass by move/*rvalue* reference and store the actual object
    ➢ Containing object has full control over member object lifetime
    ➢ Can be modified after containing object construction
    ➢ Deep copy of containing object possible by default
• An Apollo moon landing mission has-a command module and a lunar module

• Case 1: Store CM and LM as const lvalue reference
• Case 2: Store CM and LM by value, pass with move semantics
Header file: *lvalue* case

```cpp
#include "CommandModule.h"
#include "LunarModule.h"

class ApolloRef
{
public:
    ApolloRef(const CommandModule& cm, const LunarModule& lm);
    void printModuleNames() const;

private:
    const CommandModule& commandModule_;  
    const LunarModule& lunarModule_;  
};
```
Header file: \textit{rvalue} case

```cpp
#include "CommandModule.h"
#include "LunarModule.h"

class Apollo
{
public:
    Apollo(CommandModule&& cm, LunarModule&& lm);
    void printModuleName\(\) const;

private:
    // Stored by value; Apollo object now has sole ownership
    // of these member objects. They and their state can also
    // be modified as they are not restricted as const.
    CommandModule commandModule_;
    LunarModule lunarModule_;}
```
• Composition with a polymorphic member object
  • Pass by and store as const *lvalue* reference (but again, has limitations)
  • Pass by move/std::unique_ptr<> and store as unique_ptr<>
    ➢ Full control over lifetime of member
    ➢ Can replace old *clone()* methods that required object copy
    ➢ Blessed by The Creator (*A Tour of C++*, 2E)
    ➢ Google coding standards

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**Week 4: Object-Oriented Programming**
A Mercury mission (first NASA manned missions with single astronaut) was comprised of:

- A capsule

And a booster rocket:

- Redstone, for the first up-and-down missions
- Atlas, with more power for the later orbital missions
- The booster rocket is therefore a polymorphic member
• Header file:

class Mercury
{
public:
    Mercury(std::unique_ptr<MercuryBoosterRocket> booster,
            const std::string& capsule, const std::string& astronaut);

    // Rule of Five:
    // Explicitly disable copy operations:
    Mercury(const Mercury& rhs) = delete;               // 1
    Mercury& operator = (const Mercury& rhs) = delete;  // 2

    // Since we explicitly declared copy ctor and assignment
    // should also explicitly allow default move operations:
    Mercury(Mercury&& rhs) = default;                  // 3
    Mercury& operator = (Mercury&& rhs) = default;     // 4
    ~Mercury() = default;                              // 5

    void missionDetails() const;

private:
    std::unique_ptr<MercuryBoosterRocket> booster_;
    std::string capsule_;
    std::string astronaut_;}


• A gentle introduction to templates
  • functions
  • classes
• STL containers
  • sequential
  • associative
  • `std::vector<>`
    ➢ Is our sequential container of choice
    ➢ In-depth coverage of member functions
    ➢ `push_back()` vs `emplace_back()` - avoid object copy
  • `std::map<>` is useful for handling data input and reporting out results, with enum key types
• STL iterators and iterator-based `for` loops
• Range-based `for` loops
• STL Algorithms
  • Focus on `for_each()` and `transform()` to start
  • Algorithms in `<numeric>`
  • More from `<algorithm>`
  • Assignment: Use various algorithms to avoid loops (including calculations of means and dot products)

• Lambda Expressions
  • Very convenient for math!
  • As auxiliary functions in STL algorithms

• Exceptions
• Random number generation with `<random>`
  • Engines: We use Mersenne Twister 64 bit
  • Distributions: We mainly use
    ➢ Uniform
    ➢ Normal
    ➢ Student’s t

• Parallel STL algorithms from C++17
• Task-based concurrency with `std::future` and `std::async()`
  • Concurrency vs Parallelism
  • `std::async()` gets a bad rap sometimes, but
    ➢ The performance improvement is fantastic...
    ➢ Considering how easy and fool-proof it is to use
    ➢ 90%+ cut in run-time on a 20-processor virtual server
    ➢ Commonly available in modern practice
• The Monty Hall Paradox (Let’s Make a Deal)
  • Three doors marked number 1, 2, and 3
  • Behind one of the doors would be the prize, such as a new car
  • Behind the other two doors were “zonk” prizes (ie, you lose), eg a goat
The Monty Hall Paradox (continued)

• When the contestant would make a choice, say Door #1, Monty would have one of the other doors opened eg Door #3, revealing a goat

• He would then ask the contestant whether s/he would like to switch the choice to the remaining door
• The “Paradox”: If you were given the chance to switch, should you?
• It turns out the answer is yes!
• The assignment is to implement a model of the outcomes in C++, using simulations of a uniform distribution on \{1, 2, 3\}, available in `<random>`
• Eigen: Matrix Algebra Library
  • Templated/header only
  • Dynamic \texttt{MatrixXd} and \texttt{VectorXd} objects
    ➢ All standard matrix and vector operations are supported
    ➢ STL compliant
  • Matrix decompositions
    ➢ LU (Lower/Upper Triangular)
    ➢ Cholesky
    ➢ SVD (Singular Value Decomposition)
• Examples and exercises (Eigen: Matrix Algebra Library)
  • Solve system of linear equations (LU)
  • Correlated random scenarios (Cholesky + Monte Carlo)
  • Calculation of regression coefficients (SVD)
  • Rolling window predictions of portfolio returns (matrix algebra)
• Math-related components in the Boost Libraries
  • Boost Math Toolkit
    ➢ Probability Distributions: cdf, pdf, quantile functions
    ➢ Numerical Integration
    ➢ Root Solving
  • Circular Buffers
    ➢ Useful for time series and live data feeds
    ➢ STL compliant
  • Assignment: EGARCH(1, 1) “live” simulation of market volatility
    ➢ Circular buffer
    ➢ `std::normal_distribution<>` from `<random>`
• Confluence of topics covered: Use these to code realistic examples

• Pricing of financial option contracts
  • Closed form models (Derived from Black-Scholes)
    ➢ European options
    ➢ Single barrier options
    ➢ Calculate implied volatility (Boost root finding)
    ➢ Boost Math Library: Statistical Distributions (N(0, 1) cdf)
• Pricing of financial option contracts (continued)
  • Monte Carlo-based models
    ➢ European options (compare results with closed form)
    ➢ Single barrier options (compare results with closed form)
    ➢ Featured concepts:
      • Projection of asset price simulations using `<random>
      • Generation of these simulations in parallel using `std::async` and `std::future`
      • STL algorithms (including parallel algorithms)

\[ S_t = S_{t-1} e^{\left( r - \frac{\sigma^2}{2} \right) \Delta t + \sigma \varepsilon \sqrt{\Delta t} } \]
• Rcpp: An R package that provides interfaces to C++ (Dirk Eddelbuettel)
  • RcppEigen
  • BH (Boost Headers)
  • Interface to
    ➢ One-off C++ code as a faster alternative to R
    ➢ Reusable C++ code and libraries
  • For R users, calling a function in C++ is the same as calling an R function
  • Can use the powerful visualization capabilities available in R
Week 10 (Rcpp Interface)

Independent and specialized applied C++ Library

C++ Standard Library
Boost
Eigen
Other Scientific Libraries
R Code

```r
pdx <- montyHallParadox(seedCarPos = 106, seedChoicePos = 8/4, nSim = 1000)

# Set up the plot:
library(plotly)

names <- c("Stay", "Change")
x <- names
y <- pdx[2:3]
fig <- plot_ly(x = x, y = y,
               type = "bar", color = ~x)
(fig <- fig %>% layout(title = 'Monty Hall Paradox'))
```

C++ Function

```c++
// [[Rcpp::export]]
vector<int> montyHallParadox(int seedCarPos, int seedChoicePos, int nSim)
```
• At the end of the course, students can program in *modern* C++:
  • Object-oriented code
  • Efficient iterative code with STL algorithms
  • Distribution-based random number generation
  • Probability functions
  • Standard numerical methods
  • Parallelized code
  • Matrix algebra and decompositions
  • Regression models
  • Reusable library code with graphics capabilities in R
  • Real world scientific applications
    ➢ Faster than Python
    ➢ But not much more difficult

• Without ever needing:
  • *char
  • new and delete
  • Dynamic C arrays
  • Implementation of a doubly-linked list
  • Coding a binary search
  • Manual thread management or non-standard threading library

• Students are encouraged vs discouraged

• Thus making C++ a more attractive go-to language for programming scientific and mathematical applications
Thank you very much for attending!

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Sample code will also be made available on GitHub